# Combining Quality Measures of Association Rules with Applications in Distributed Web Log Mining

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**Abstract.** In this paper, we propose a technique for to combine two or more pairs of quality measures for association rules in order to obtain a better pair of quality measures. This combining method can be used to mining association rules from distributed databases. Also, the paper presents an use case for mining association rules from distributed WWW servers access logs, using proposed measures. Reasoning on web logs on the base of association rules might be an attempt to produce personalized content on commercial web sites and portals without storing explicitly of the user-profile information.

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### 1 Introduction

Association rules provide a means for representing dependencies between attribute value objects (data records) stored in a (distributed) database. Association rules show attribute value conditions that occur frequently together in a given dataset.

Let  $\mathcal{D} = \{x_1, \dots, x_n\}$  be a transactional database contains records described by a set of binary attributes (items)  $\mathcal{I}$ . For a specified transaction  $x \in \mathcal{D}$  we will retrieve the value of attribute  $A \in \mathcal{I}$  using A(x). This value is either 1 or 0 indicating whether or not item A bought in transaction x.

Typically, an association rule involve two sets, A and B, of attributes and has the following form  $A \rightharpoonup B$ . The meaning of a rule  $A \rightharpoonup B$  is that when A is bought in a transaction, B is likely to be bought as well.

An example of an association rule is: " 70% of clients who bought printers also bought paper".

The quality of an association rule is expressed by several measures, among which *support* and *confidence* are two essential ones [2]. The *support* is the

number of transactions in which both A and B occurs and the *confidence* represents the percentage of transactions containing A that contain B as well.

In this paper, starting from two pairs of quality measures, we propose a technique for their combining in order to obtain a new pair. The associativity of combining operation allow us to mine association rules from distributed databases. We give an application in mining association rules from distributed WWW servers access logs.

## 2 Overview of the support and confidence measures

Let  $\mathcal{D}$  be a non-empty database containing records described by theirs values binary attributes. We will denote by  $D_A$  the set of all transactions x in which A was purchased, i.e.

$$D_A = \{ x \in \mathcal{D} | A(x) = 1 \};$$

in this way  $D_A$  is a subset of  $\mathcal{D}$ . We denote by  $coD_A$  the set of transactions that not contain the item A, i.e

$$coD_A = \{x \in \mathcal{D} | A(x) = 0\}.$$

**Definition 1 (Support).** The support of an association rule  $A \rightharpoonup B$  is usually defined as:

$$supp(A \rightharpoonup B) = \frac{|D_A \cap D_B|}{|\mathcal{D}|}$$

where  $|D_A|$  is the number of transactions that contain A.

The classical confidence is usually defined as below:

**Definition 2 (Confidence).** The confidence of an association rule  $A \rightarrow B$  is usually defined as:

$$conf(A \to B) = \frac{|D_A \cap D_B|}{|D_A|} \tag{1}$$

The need for more refined confidence measures appears frequently in practical applications. Therefore others confidence measures were proposed by Hullermeier [8]. He suggested a formal framework for the systematic derivation of quality measures which is based on the classification of stored data into examples of a rule, counterexamples of that rule, and irrelevant cases. The result is the definition of classical n-confidence:

$$conf_n(A \to B) = \frac{|D_A \cap D_B|}{|D_A \cap coD_B|}$$
 (2)

Later De Cook et al. in [3] defined pessimistic (p) confidence and optimistic (o) confidence:

$$conf_p(A \rightharpoonup B) = \frac{|D_A \cap D_B|}{|coD_A \cup coD_B|}$$
(3)

$$conf_o(A \rightharpoonup B) = \frac{|coD_A \cup D_B|}{|D_A \cap coD_B|} \tag{4}$$

They introduce these measures in order to capture incompletion cases. For example in the case of the rule "if X buy bread then X buy also butter", when determining the pessimistic confidence of a rule we have the following assumption in mind: if those people who did not buy bread, would have bought bread, they would not have bought butter as well. For the optimistic confidence measure on the other hand we assume that if those people who did not buy bread, would have bought bread, they would have bought butter as well.

An interesting relation between these measures is the following:

Proposition 1. (De Cock et al. [3])

$$conf_p(A \rightharpoonup B) \le conf_n(A \rightharpoonup B) \le conf_o(A \rightharpoonup B)$$

### 3 Combining quality measures

In this section we will consider pairs of quality measures  $(M_*, M^*)$  that verify the following property:

$$M_* < M^*$$

i.e. quality measures verifying relationships such as one from Proposition 1.

According with the relations (2),(3), (4) and the proposition 1 we introduced in [9] and finalized in [10] a collection of such measures. For instance:

1.  $(conf\_po_*, conf\_po^*)$ 

$$conf.po_*(A \rightharpoonup B) = \frac{|D_A \cap D_B|^2}{|D_A \cap D_B|^2 + |coD_A \cup coD_B|^2}$$

$$conf.po^*(A \rightharpoonup B) = \frac{|coD_A \cup D_B|^2}{|coD_A \cup D_B|^2 + |D_A \cap coD_B|^2}$$

2.  $(conf\_pn_*, conf\_pn^*)$ 

$$conf\_pn_*(A \rightharpoonup B) = \frac{|D_A \cap D_B|^2}{|D_A \cap D_B|^2 + |D_A \cap coD_B| \cdot |coD_A \cup coD_B|}$$

$$conf_{-}pn^*(A \rightharpoonup B) = \frac{|D_A \cap D_B| \cdot |coD_A \cup D_B|}{|D_A \cap D_B| \cdot |coD_A \cup D_B| + |D_A \cap coD_B|^2}$$

are such measures.

By analogy with Dempster's rule for combining the degrees of belief and plausibility from evidence theory [14], for to combine two pairs of confidence

measures  $(M_{1*}, M_{1}^*)$  and  $(M_{2*}, M_{2}^*)$ , with  $M_{1*}, M_{1}^*, M_{2*}, M_{2}^* \in [0, 1]$ , we propose the following formula

$$\widetilde{M}_* = \frac{M_{1*}M_2^* + M_1^*M_{2*} - M_{1*}M_{2*}}{1 - M_{1*}(1 - M_2^*) - M_{2*}(1 - M_1^*)}$$
(5)

$$\widetilde{M}^* = \frac{M_1^* M_2^*}{1 - M_{1*} (1 - M_2^*) - M_{2*} (1 - M_1^*)}$$
(6)

The measures introduced by (5) and (6) define an associative<sup>1</sup> composition operation (i.e. a combination rule)  $\circ$ :

$$(M_{1*}, M_{1}^{*}) \circ (M_{2*}, M_{2}^{*}) = (\widetilde{M}_{*}, \widetilde{M}^{*})$$

In addition the following relations hold:

$$\widetilde{M}_* < \widetilde{M}^*$$
 and  $\widetilde{M}^* - \widetilde{M}_* < \min\{M_1^* - M_{1*}, M_2^* - M_{2*}\}.$ 

Therefore, from a pair  $(M_1, M_2)$ ,  $M1 \leq M_2$ , we can define a single measure:

$$M = \lambda_1 \cdot M_1 + \lambda_2 \cdot M_2$$
, with  $\lambda_1 + \lambda_2 = 1$ 

where  $\lambda_1$  and  $\lambda_2$  represent the belief degree in  $M_1$  respectively in  $M_2$ .

Example 1. Consider the following sample transaction database presented in Table 1. The  $\widetilde{M}_*$  and  $\widetilde{M}^*$  are computed for the pairs  $(conf\_po_*, conf\_po^*)$  and

TID	$I_1, I_2, I_3, I_4, I_5$	TID	$I_1, I_2, I_3, I_4, I_5$	TID	$I_1, I_2, I_3, I_4, I_5$
$T_1$	1, 0, 1, 0, 0	$T_7$	0, 0, 1, 1, 1	$T_{13}$	1, 1, 1, 0, 1
$T_2$	1,0,1,0,0	$T_8$	1,0,0,1,0	$T_{14}$	0, 1, 1, 0, 1
$T_3$	0, 0, 1, 0, 1	$T_9$	0, 1, 0, 1, 1	$T_{15}$	1, 0, 1, 0, 1
$T_4$	1, 1, 0, 1, 0	$T_{10}$	0, 1, 1, 1, 0	$T_{16}$	0, 1, 1, 0, 0
$T_5$	1, 1, 1, 0, 1	$T_{11}$	1,0,0,1,1	$T_{17}$	1, 1, 0, 1, 0
$T_6$	1,0,0,0,1	$T_{12}$	1, 1, 0, 0, 1	$T_{18}$	1,0,1,1,1

Table 1. A database sample

 $(conf\_pn_*, conf\_pn^*)$  and The table 2 shows the values obtained for quality measures above presented.

### 4 Web Log mining use case

The Web Log mining use case was widely studied in the context of adaptive web sites and services. A number of papers such as [5], [13] and [12] address

This permits to combine an arbitrary number of measures

Rule	$conf\_po_*$	$conf\_po^*$	$conf\_pn_*$	$conf\_pn^*$	$\widetilde{M}_*$	$\widetilde{M}^*$
$I_1 \rightharpoonup I_3$	0,200	0,800	0,077	0,667	0,196	0,581
$I_2 \rightharpoonup I_3$	0,129	0,925	0,088	0,814	0,180	0,776
$I_4  ightharpoonup I_1$	0,129	0,962	0,114	0,893	0,214	0,874
$I_3, I_5  ightharpoonup I_1$	0,075	0,962	0,087	0,870	0,145	0,847
$I_1, I_4  ightharpoonup I_3, I_5$	0,003	0,925	0,014	0,467	0,015	0,433
$I_1 \rightharpoonup I_4, I_5$	0,015	0,390	0,012	0,138	0,007	0,055

**Table 2.** Values for quality measures  $\widetilde{M}_*$ ,  $\widetilde{M}^*$ 

this scenario with different techniques. In this section we use the same scenario by addressing the quality measures combination issues i.e. by using proposed measures (5) and (6).

One natural assumption is that the server access logs contain users requested files into a chronologically order. The Table 3 shows a fragment of Apache Web server.

```
220.226.35.198 - - [23/Feb/2007:15:54:10]

"GET /products/product-A.html HTTP/1.1" 200 12482

220.226.35.198 - - [23/Feb/2007:15:54:12]

"GET /products/images/A.jpg HTTP/1.1" 200 12482

216.122.48.128 - - [23/Feb/2007:18:43:51]

"GET /library.html HTTP/1.1" 200 42227

220.226.35.198 - - [23/Feb/2007:15:54:10]

"GET /products/product-B.html HTTP/1.1" 200 15482

172.30.110.140 - - [23/Feb/2007:21:28:01]

"GET / HTTP/1.0" 200 23903

195.113.25.239 - - [23/Feb/2007:22:46:55]

"GET /html/d711.html HTTP/1.1" 200 4513
```

Table 3. A fragment of Apache Web Log

Typically, these web server logs contain millions of records therefore they are appropriate to mine association rules and then use them in the context of web sites personalization. Another argument in the favor of using association rules is that the logs are never complete and exhaustive therefore the conclusions cannot be derived using standard first order logic. Technically, for each visit, web log records the remote users host name or IP address, the time when the request arrived, the HTTP method (GET, POST, etc.) the remote user used, the URL of the visited web document, the status code of the HTTP response (for example: 200 for successful access, 404 for file not found), and the number of bytes returned to the user (in most cases is the document size).

For a given web server log the mining process start with a preprocessing row data. The fist step is a clean process [11]. When a web page is requested by user then automatically all images, clips embedded in page are recorded in web access log. These records can be removed because are irrelevantly for mining process.

The next step is to extract user sessions from web logs. A user session is a relatively independent sequence of web requests from the same user. We consider web log data as a sequence of distinct web pages, where subsequences, such as user sessions can be observed within unusually long gaps between consecutive requests.

For example, assume that the web log consists of the following user visit sequence:

User IP	Date	Requested Page	User IP	Date	Requested Page
$IP_1$	00:00:00	A	$IP_1$	00:00:19	E
$IP_2$	00:00:05	В	$IP_2$	00:00:25	A
$IP_3$	00:00:10	D	$IP_1$	01:00:19	E
$IP_1$	00:00:15	С	$IP_1$	01:02:10	A

Table 4. Visited page sequence

User IP	Session	User IP	Session	
$IP_1$	A, C, E	$IP_3$	D	
$IP_2$	B, A	$IP_1$	E, A	

Table 5. User sessions

The Table 5 shows users sessions according to user IP's. Using association rule discovery techniques we can find correlations such as:

50% of clients who accessed the Web page with URL /products/product-A.html also accessed /products/product-B.html

or

35% of clients who accessed /special-offers.html placed an online order in /products/product-C.html

Discovery of such rules for online shops can help in the development of effective marketing strategies. Also, association rules discovered from WWW access logs can give an indication of how to better organize the organization's Web space.

For example, if one discovers that

80% of the clients accessing /products and /products/product-A.html also accessed /products/product-B.html,

but

only 30% of those who accessed /products also accessed /products/product-B.html, then it is likely that some information in product-A.html leads clients to access product-B.html.

This correlation might suggest that this information should be moved to a higher level (e.g., /company/products) to increase access to /products/product-B.html

At this date the majority of WWW serves have mirrors for reducing the pages access time and avoid their overloading. In this situation the concern is for determining association rules for the web pages. A simple and coarse solution would be to keep all the log data from these servers in a single place and to apply a standard association rules determination algorithm. This approach is inefficient due to the large size that these logs can have.

Our proposal is: Let suppose we have two servers S1 and S2. By applying the standard association rules determination algorithm we can find, for every server, a set of association rules between pages together with their attached confidence pairs  $(P_{1*}, P_1^*)$  and  $(P_{2*}, P_2^*)$ , respectively. On this basis we can compute a common set of rules by combining the S1 and S2 rules according to (5) and (6) formulas.

#### 5 Conclusions

In this paper we propose a combining technique of two pairs of measures. This combining technique is useful for evaluate quality of association rules that rise from different sources. The obtained results can be extended to fuzzy association rules, similarly with papers [3], [4], [6]. Potential applications can be used by encoding association rules into a web rule language such as RuleML [1], [17] or R2ML [15], [16] which will permit a web distributed architecture of association rules repositories covering different subjects. Builders of portals as well as commercial web sites may use these rules to create user-specific content. Some efforts on that are already done but specifically in the Semantic Web area [7] and their main criticism is that they adopt a non-distributed solution of user profiles.

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